

Partitions.

Two dimensional Essay.

$$-xy \rightarrow \max \text{ such that } x + y = \frac{3}{4}$$

$$\begin{bmatrix} -x \\ -y \\ 0 \end{bmatrix} = \lambda \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} \text{ with } x = y = z = -\lambda \text{ and } \frac{3}{4} = x + y$$

$$\lambda = -\frac{3}{8} = x = y$$

Three dimensional Essay.

$$-xyz \rightarrow \max \text{ such that } x + y + z = \frac{3}{4} + \frac{1}{8} = \frac{7}{8}$$

$$\begin{bmatrix} -x \\ -y \\ -z \\ 0 \end{bmatrix} = \lambda \begin{bmatrix} 1 \\ 1 \\ 1 \\ 0 \end{bmatrix} \text{ with } x = y = z = -\lambda \text{ and } \frac{7}{8} = x + y + z = 3(-\lambda)$$

$$\lambda = -\frac{7}{24} = x = y = z$$

Four dimensional Essay.

$$-xyzv \rightarrow \max \text{ such that } x + y + z + v = \frac{3}{4} + \frac{1}{8} + \frac{1}{16} = \frac{15}{16}$$

$$\begin{bmatrix} -x \\ -y \\ -z \\ 0 \end{bmatrix} = \lambda \begin{bmatrix} 1 \\ 1 \\ 1 \\ 0 \end{bmatrix} \text{ with } x = y = -\lambda \text{ and } \frac{15}{16} = 4(-\lambda)$$

$$-\lambda = -\frac{15}{240+24} = \frac{15}{64} \quad x = y = z = v = \frac{15}{64}$$

We have the following results:

$$\begin{bmatrix} 1 & 1 \\ 2 & \frac{3}{8} \\ 3 & \frac{7}{24} \\ 4 & \frac{15}{64} \end{bmatrix}$$

